

Sketch a graph of the function from the given information.

$$f(7) = 6, f(-3) = 3, f(8) = 3, f(10) = 4,$$

$$f(5) = 5.5, f(-5) = 4, f(5) = f(0) = \text{undefined}$$

$$f'(7) = f'(-3) = f'(2) = f'(8) = 0$$

$$f'(x) > 0 \text{ for } (-\infty, -7) \cup (-3, 0) \cup (8, \infty)$$

$$f'(x) < 0 \text{ for } (-7, -3) \cup (0, 5) \cup (5, 8)$$

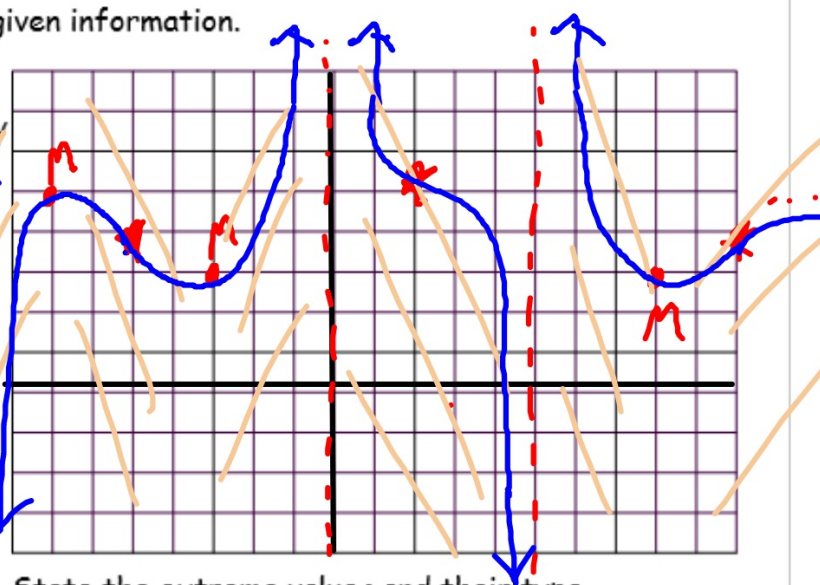
$$f''(5) = f''(2) = f''(10) = 0$$

$$f''(x) > 0 \text{ for } (-5, 0) \cup (0, 2) \cup (5, 10)$$

$$f''(x) < 0 \text{ for } (-\infty, -5) \cup (2, 5) \cup (10, \infty)$$

$$f(x) = \infty, \lim_{x \rightarrow 0^+} f(x) = \infty, \lim_{x \rightarrow 5^-} f(x) = -\infty,$$

$$f(x) = \infty, \lim_{x \rightarrow \infty} f(x) = 5$$



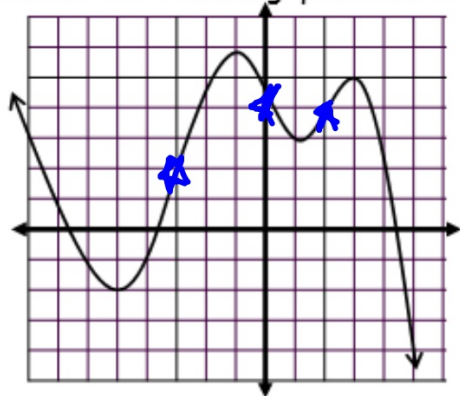
State the extreme values and their type.

$$\text{POI: } (-5, 4), (2, 5.5), (10, 4)$$

$$\text{Rel. Min: } (-3, 3), (8, 3)$$

$$\text{Rel. Max: } (-7, 6)$$

2. Answer the following questions using the given graph. (values will all be approximate)



$$f'(x) > 0: (-5, -1) \cup (1, 3)$$

$$f'(x) < 0: (-\infty, -5) \cup (-1, 1) \cup (3, \infty)$$

$$f''(x) > 0: (-\infty, -3) \cup (0, 2)$$

$$f''(x) < 0: (-3, 0) \cup (2, \infty)$$

Extreme Values: R. Min: $(-5, -2)$ / R. Max: $(1, 3)$

Points of Inflection: $(-3, 2), (0, 4.5), (2, 4)$

Discontinuities: _____

Does the Mean Value Theorem apply for the given interval? If so, calculate the value(s) of c .
If not, state the reason why.

3) $f(x) = x^2 + 3x - 1$ $[-3, 1]$

$$(-3, -1)(1, 3)$$

$$m = \frac{3 - -1}{1 - -3} = \frac{4}{4} = 1$$

$$) = 2x + 3 = 1$$

$$2x = -2$$

$$\textcircled{x = -1}$$

4) $f(x) = x^2 - 5x + 7$ $[-1, 3]$

$$(-1, 13)(3, 1)$$

$$m = \frac{1 - 13}{3 - -1} = \frac{-12}{4} = -3$$

$$f'(x) = 2x - 5 = -3$$

$$2x = 2$$

$$\textcircled{x = 1}$$

$$5) f(x) = x^3 - 6x^2 + 9x + 2 \quad 0 \leq x \leq 4$$

$$0, 2) (4, 6)$$

$$m = \frac{6-2}{4-0} = \frac{4}{4} = 1$$

$$1 = 3x^2 - 12x + 9 = 1$$

$$3x^2 - 12x + 8 = 0$$

$$\frac{\sqrt{144 - 4 \cdot 3 \cdot 8}}{6} = \frac{12 \pm \sqrt{48}}{6}$$

$$\frac{4\sqrt{3}}{3} = \frac{6 \pm 2\sqrt{3}}{3} = (0.845, 3.155)$$

$$6) f(x) = \frac{x+2}{x} \quad [-1, 2]$$

Not continuous

b/c VA at $x=0$

Does the Mean Value Theorem apply for the given interval? If so, calculate the value(s) of c . If not, state the reason why.

7) $f(x) = x^4 - 16x^2 + 2$ $-1 \leq x \leq 3$

$(-1, 13)$ $(3, -61)$

$$m = \frac{-61 - 13}{3 - (-1)} = \frac{-74}{4} = -18.5$$

$$= 4x^3 - 32x = -74$$

$$4x^3 - 32x + 74 = 0$$

$$x = .382, 2.618$$

↓ on calc.

8) $f(x) = \frac{1}{3}(x^3 + x - 4)$ $[-1, 2]$

$(-1, -2)$ $(2, 2)$

$$m = \frac{2 - (-2)}{2 - (-1)} = \frac{4}{3}$$

$$f(x) = \frac{1}{3}x^3 + \frac{1}{3}x - \frac{4}{3}$$

$$f'(x) = x^2 + \frac{1}{3} = \frac{4}{3}$$

$$x^2 - 1 = 0$$

$$x = \pm 1$$

$$9) f(x) = \frac{x+2}{x} \quad [2, 5]$$

$$2, 2) (5, 1.4)$$

$$\frac{1.4 - 2}{5 - 2} = \frac{-0.6}{3} = -0.2$$

$$\frac{-(x+2) \cdot 1}{x^2} = \frac{-2}{x^2} = -0.2$$

$$= \sqrt{10}$$

$$-2 = -0.2x^2$$

$$10 = x^2$$

$$x = \pm \sqrt{10}$$

$$10) f(x) = \sin(x) - \frac{1}{2}x \quad -\pi \leq x \leq \pi$$

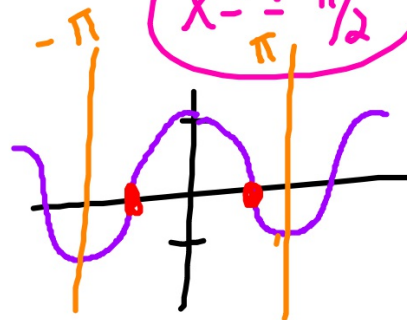
$$(-\pi, 1.571) (\pi, -1.571)$$

$$m = \frac{-1.571 - 1.571}{\pi - -\pi} =$$

$$f'(x) = \cos(x) - \frac{1}{2} = -\frac{1}{2}$$

$$\cos(x) = 0$$

$$x = \pm \pi/2$$

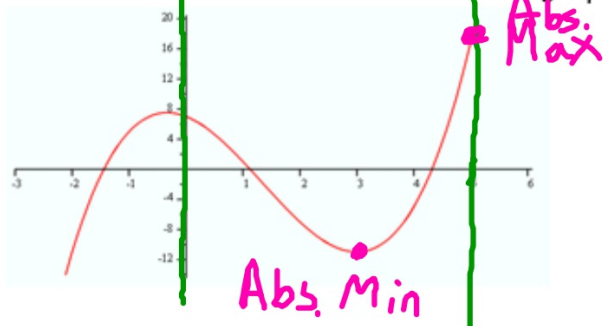


Using the Min/Max Existence Theorem determine the minimum and maximum values.

11) $f(x) = x^3 - 4x^2 - 3x + 7$ $0 \leq x \leq 5$

12) $f(x) = \frac{1}{3}(x^3 + x - 4)$ $[-1, 2]$

Label the absolute max and min on the graph.



$$f(x) = \frac{1}{3}x^3 + \frac{1}{3}x - \frac{4}{3}$$

$$f'(x) = x^2 + \frac{1}{3} = 0$$

$$x^2 = -\frac{1}{3}$$

$\emptyset$

$$f(-1) = -2 \text{ Min}$$

$$f(2) = 2 \text{ Max}$$

$$13) f(x) = \frac{x}{x-3} \quad [-1, 4]$$

not continuous b/c
VA at $x=3$

$$14) f(x) = x^2 + 3x - 1 \quad [-3, 1]$$

$$f'(x) = 2x + 3 = 0$$

$$x = -3/2$$

$$f(-3) = -1$$

$$f(-3/2) = -3.25 \quad \text{Min}$$

$$f(1) = 3 \quad \text{Max}$$

